



On the theory of glacial erosion in valleys

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1 Erosion theory and theory of glacier movement

In contrast to the phenomena of regional or even continental scale glaciations, which are generally independent of the subglacial relief (e.g. plateau glaciation, ice sheets), local-scale glaciations usually adapt to a previously-formed valley relief. In this case, ice movement is directed by such valleys which in the process become reshaped to a greater or lesser extent, so that, after the ice has disappeared, they can be clearly distinguished from valleys that have remained un-glaciated.

The understanding of the natural laws governing these morphological changes, referred to as the theory of glacial erosion in valleys, has been the subject of lively discussions and significant controversy, especially in the period between about 1900 and 1935. Many of the most renowned geographers and geologists have been involved (cf. the bibliography). However, if one opens a modern handbook of glaciology, geomorphology or glacial geology, such as the works by von Drygalski and Machatschek (1942), Maull (1938) and von Klebelsberg (1948), one will search in vain for a physical theory of glacial erosion in valleys. Despite partial progress in illuminating some principles of glacial valley formation, so far, these efforts have not yet yielded a comprehensive physical theory of glacial erosion.

A major problem is still to find an explanation for the presence of bedrock steps and basins within valleys that have been strongly shaped by glaciers. The transverse profile of such valleys formed in solid rock, if still intact and not covered by material, often feature in their entirety or at least in the lower parts smoothed walls and U-like cross-sections, and are referred to as trough valleys.

A physically plausible theory for the formation of steps within trough valleys is provided through Albrecht Penck's¹ theory of confluence and diffluence steps, which is based on the understanding that glacial valleys are bedforms generated by ice streams. At the same time the understanding that many of these transverse bedrock ridges and glacial staircases were caused by differences in lithology within the glacial valleys is undoubtedly also well-founded. However, the works of Distel (1912), Lehmann (1920), Lautensach (1912), de Martonne (1910a, b), and Sölch (1935) have now shown convincingly that by no means all of the transverse ridges and steps, and especially not the most significant ones within the glacial valleys, can have formed as a result of glacial confluence,

¹Note by editor: The author most likely refers to Penck and Brückner (1909) as listed in the references.

diffluence or lithological differences. While more subdued valley knickpoints often find a plausible interpretation in one of the aforementioned factors, the more pronounced valley steps are undoubtedly also linked to pre-existing breaks in valley slope from the time before the valley was glacier filled. De Martonne (1910a, b), Lautensach (1912), Lehmann (1920) and others have therefore taught that the work by valley glaciers often accentuated pre-existing breaks in valley gradient, while at the same time imprinting its typical U-shaped valley cross-section. This occurs in such a way that ridges and troughs develop along the longitudinal profile, and that this process contributes greatly to the overall shaping of landforms in the glacial valleys. These ideas have received broad approval, even if there remain differences regarding the quantitative assessment of the glacial activity. However, these authors, and in particular de Martonne (1910a, b) and Burchard (1923), have not succeeded in establishing even a roughly satisfactory physical interpretation of the abovenamed finding. I will refrain here from pointing out the mathematical-physical inconsistencies contained in the formulae established by de Martonne (1910a, b) and Burchard (1923) to explain glacial erosion. This has been sufficiently demonstrated by Lautensach (1912) and Burger (1933). Burger's own work contains deeper insights but I believe these too have not yet penetrated to the core of the matter. The latter appears to me to be the following:

Previous theoretical attempts to explain glacial erosion in valleys were based exclusively on the idea that ice movement can be compared approximately to the movement of an ideal, albeit very viscous, fluid with an approximately laminar flow. This is the idea on which Finsterwalder (1897) based his geometric theory of glacier movement with such great success, and which was also used by Weinberg (1907), Somigliana (1921, 1931) and Lagally (1933, 1939).

This model, however, includes some very serious preconditions and it is worthwhile to consider to what extent it is likely that these can be always at least be approximately fulfilled in nature. The normal relationship of a liquid, even a viscous one, to its vessel walls is that the internal friction of the liquid, i.e., the friction of the liquid particles against each other, is less than the friction of the liquid against the walls of the vessel. In the case of slow laminar flow, the boundary layer of the liquid against the vessel must be almost motionless because of the increased friction there. The speed of movement of the liquid must therefore decrease from the inside of the liquid towards the vessel wall, and thereby more or less tend towards the value zero.

Based on the corresponding assumption that ice movement across the glacier bed would be almost non-existent, it is theoretically logical to hold the view, as is done by some researchers, that the glacier exerts little work on its bed, but instead may actually have an almost conserving effect on its underlying bedrock. However, the same assumption has important consequences for the idea of glacier movement in a valley with spatially varying cross-sections. For example,

where steps in the underlying morphology of a viscous fluid flow are present, these steps will at least somewhat be noticeable on the surface of the flow, albeit not with the full height of the step hidden at the underlying bed. Above the step, therefore, there must be a reduction in the overall flow cross-section and thus, in order to maintain the overall flow, an increase in the average flow velocity. This must inevitably also cause at least a slight increase in base velocity of the viscous liquid flow. Conversely, at the bottom of the step, on the other hand, an increased cross-section and thus a slowing fluid flow can be expected. Under such conditions, every realistic quantitative model should yield areas of increased erosion in the zone over the steps and reduced erosion at the foot of the steps. The increased surface area of the viscous liquid above the hidden edge of the steps proves that more potential energy of the liquid per unit area is required for the flow process than at other points further up- and downvalley. This increased energy consumption will also enhance friction during the flow process, which in turn will lead to increased basal friction. Thus, according to this view, existing breaks of slope and steps in the valley longitudinal profile should slowly be removed by glacier activity and not further morphologically enhanced. Lautensach (1912) has already pointed this out. The same would also be derived when using the formulae, if corrected, by de Martonne (1910a, b) and Burchard (1923). However this means, that this theory predicts the opposite of what is actually evident from field observation.

A number of other observational facts, however, indicate that the movement of ice should not be regarded as the movement of a normal viscous fluid, or at least not in most cases (Demorest, 1943; Streiff-Becker, 1938; Seligman, 1947). This is also the direction of the discussions based on laboratory work carried out mainly in England. Perutz (1947) states that the theory of viscous fluids can only be applied to glacier movement in exceptional cases, because ice does not have a constant viscosity but one that varies considerably with stress ratio, temperature and crystal orientation and thus behaves more like a plastic body. Orowan (1949) also believes that a more realistic picture will be achieved by replacing the viscous liquid model with the idea of a plastic body. Under certain conditions ice represents a substrate that hardly deforms, but when a critical shear stress is exceeded, it can deform to a large extent. These thoughts come close to the view long held by von Drygalski (1898) and von Drygalski and Machatschek (1942).

According to these views, and based on laboratory experiments and the interpretation of field observations, Finsterwalder (1950) argues for a critical value of shear stress of the ice. Above this value ice changes its consistency due to overstressing, which is still dependent on special conditions, e.g., temperature. Observations of glaciers with high flow velocities in relation to the cross-section from various parts of the world reveal a form of movement which Finsterwalder (1931, 1937) and Finsterwalder and Pillewitzer (1939) called block floe movement. Characteristic of this is a large increase in ice velocity at the edge, probably also at the bottom of the glacier, so that the main mass of the ice moves forward at a fairly uniform speed, similar to a rigid mass, while parts of the ice, e.g., at the edge or at blind angles, hardly seem to move at all, separated from it by narrow sections of increased elasticity. The block thrust mass itself breaks in places into floes during movement, namely over irregularities in the bedrock, occasionally to the point of serac formation.

The difference between the two views of plastic deformation and block floe movement is perhaps less significant than it appears at first glance. For localised areas of increased flexibility of the ice, especially in the marginal and nearground parts of the ice mass, observed by Finsterwalder and Pillewitzer (1939) and Finsterwalder (1950) and termed as favourable concomitants of block floe movement that occurs on irregularly shaped rock beds. On the other hand, Demorest (1943) and Streiff-Becker (1934, 1941) developed the concept of plastic deformation and squeezing of the glacier ice, especially for parts of plateau ice masses located deeper below the surface, because they found the superficial parts of the ice, in view of the continually added ice mass there and the overall stationary state, to move less than should be expected. Another characteristic of the glaciers is the occurrence of very considerable fluctuations in the surface slope. In many cases, the ice surface, which is inclined differently from place to place, virtually reproduces the irregularities present in the underground, such as steps and the like, albeit to a lesser degree. The flow velocity is comparatively little increased on the steep sections.

This can only be understood under the assumption that the rheology of the glacier as a whole is extraordinarily rigid and, in any case, greater than the outward friction with the glacier bed. For if the external friction with the underground were greater than the internal friction of the flowing mass, the flowing mass would fill up all bedrock concavities and pass over basal bedrock steps by maintaining a largely even surface gradient. By contrast, the glacier movement can also be viewed as a compact push of ice along the bed with relatively small changes in the cross-section of the glacier or alternatively a sliding over the glacier bed, which appear to be facilitated by increased plasticity of the basal ice portion. This model has more in common with a body that is highly flexible in a longitudinal direction, resting on a lubricant over the base, while maintaining a largely unchanged cross-section, as represented by a stream formed by more or less rigid individual bodies with reduced basal friction, than would be the case with a viscous fluid adhering to the channel walls.

The famous drill rod results from the Hintereisferner presented by Hess (1924, 1929) point in the same direction. The relatively low inclination of the drill rods in the 214 m deep borehole following their thawing out after 18 years led Hess to assume that the basal velocity of the glacier only marginally lags the surface flow velocity of the glacier. This suggests, that the internal friction of the glacier must be high compared to the external friction. Because in case of an ideal viscous fluid in laminar motion, the flow velocity should approach zero towards the underground because of the strong ground friction. In this respect too, the movement of the glacier appears to resemble a movement by a stream comprising rigid individual bodies along its bed.

2 On the theory of basal stress by a stream of detached blocks

This consideration leads us to examine the theoreticallyexpected stress on the ground that would be exerted by a stream of rigid individual bodies². We believe that a series of adjacent cuboid-like ice bodies is pushed forward along an inclined path by a force acting vertically everywhere (gravity) (Fig. 1). In each of the rigid cuboids, the force can be thought of as acting at the centre of gravity. This force can be deconstructed into two components, perpendicular and parallel to the surface. It follows, that in such a system, the steeper the underlying surface is inclined, the more of the downward pressure is transferred into the slope-parallel force components. At the same time, the force component acting vertically on the steep slope is equal for all participating bodies.

A different picture, however, emerges for the cuboid bodies located at the foot of the steep slope, right at the transition to a flattening surface (block 4 in Fig. 1). In this case, a large part of the force transmitted parallel to the slope from uphill now suddenly takes part in the action perpendicular to the flattened underlying surface and is added as a strong additional component to the locally resulting force pressing at right angles to the ground. The next downward following cuboid, however, receives from above only the force component parallel to the ground in relation to the new ground inclination and shows only the right-angled part of the local vertical force as ground pressure.

One can also express the conditions in another way. As a result of the great ice rigidity and its relatively low ground friction, the inclined ice column over the steep slope rests on the foot of the slope, almost as if it were rigid. Here, a particularly strong stress will be exerted on the subsurface, and thereby erosion and undercutting.

Of course, ice is never completely rigid. In reality, the ice column lying on the slope thickens towards the bottom. But the fact that it does not flow completely apart until reaching a balance between the glacier surface above and below the steepened slope, and considering the relatively low friction at the glacier bed, forces us to conclude that a transfer of pressure through the ice column towards the foot of the slope takes indeed place.

²The following train of thought was already briefly hinted at in a discussion note at the International Geographical Congress in Amsterdam in 1938.



Figure 1. Schematic sketch depicting the ground pressure of an idealized ice stream of rigid individual cuboid bodies at varying surface slopes. Note in particular the differences in size of the "force component normal to the slope" for cuboids 4 and 7 compared to the other cuboid blocks.

From our concept of a moving flow of rigid individual blocks of ice, results the understanding of a significantly increased stress acting directly upon the foot of a slope. This theoretical result is also in agreement with the overdeepened troughs observed in glacially formed valley landscapes at the foot of cirque walls and valley steps. It is needless to add that such deepenings at the lee side of bedrock obstacles is ultimately limited in extent. This is because the developing counter-slope on the opposite (downvalley) side of the depression below the valley step, would eventually lead to such a strong increase in basal friction that the ice movement over the ground thus the erosion of the subsurface would decrease significantly.

Special conditions again exist at the upper cuboid ice body at the beginning of a new slope steepening (block 7 in Fig. 1). Here the force component transmitted from above and parallel to the upper, flatter slope now becomes a force directed away from the steepening slope towards the air. This additional force transmitted from above must therefore have an effect in form of a reduction in the ground pressure of this cuboid. Indeed, theoretically it could lead to the toppling of this cuboid from the support surface, which can also be seen in practice by imitating the described arrangement, e.g., with toy blocks.

This fact, too, is undoubtedly important for understanding the observational facts available on glacial erosion in valleys. Also, we consider it of considerable importance for explaining the formation of cirque and other sills (ridges) so often observed in glacial valleys, evidencing locally reduced ice erosion at the uppermost point of a slope.

Reduced ice erosion at the top of the steps and increased erosion at the foot of the steps are basic prerequisites for the theory of increasing pre-existing morphological bed irregularities by valley glaciers. By contrast, this theory is not compatible with the idea of glacier movement as represented by a viscous fluid. So far the issue has remained unresolved. The idea of glacier movement in the manner of a stream of rigid blocks, on the other hand, provides real justification for the assumptions underlying the glacial morphological theory for the interpretation of available observations. This seems to me to be its particular merit.

It seems necessary to point out that our ideas about the basal stresses of a flow comprising rigid bodies of ice slope knickpoints are essentially independent of whether or not the glacier block flow rests directly on its bed or if, according to the assumptions of Drygalski and modern glaciologists, a intermediate zone of greater plasticity occurs between the blocks and the glacier bed. Where the basal or wall pressure of the block floe flow is locally particularly high, as based on slope gradient or cross-sectional conditions, the intermediate zone of higher plasticity would either be squeezed away so that the rigid block touches the bed itself, or the plasticised masses would be pressed past such points with greatly increased speed. In both cases, there would be an increased stress on the bed wall at the points in question, at least according to all the previous experience of the effect of glacial ice on rock.

The idea developed by Ampferer (1904) that a glacier, especially in narrow valleys, is to be regarded as a rigid mass bearing down on the valley slopes on both sides with arch pressure and moving down the valley, is also not far removed from our idea of a block slab flow.

With the above stated ideas, we do not intend to suggest that a glacier as such constitutes a stream of rigid individual bodies. Rather, we seek to express that valley glaciers occupy a peculiar intermediate position between a viscous fluid and a stream of rigid individual bodies. In fact, glaciers appear to combine characteristics from both end members. According to the results of Finsterwalder (1950), they seem to behave more like viscous liquids when the ice moves slowly relative to the ice cross-section, and more like block floe flows when the ice moves relatively quickly. For the erosional capacity of valley glaciers, however, it is precisely the peculiarities corresponding to the analogy of a stream of rigid individual bodies, which have received less attention so far, and which are therefore of particular importance here.

The successes with regard to determining glacier volume and mass balance achieved for slow-flowing glaciers on the basis of velocity measurements and geometry leave little doubt that the glacier model of a viscous fluid comes very close to reality. Consequently, one should also conclude that glaciers of such type have only a modest sculpturing effect on their underground and will thus not enhance slope breaks on the valley floor.

The glaciers with block flow movement (detached blocks) behave differently. It appears to us that these glaciers of this type are the actual agents generating the stark variety of erosional landforms forms within glacial valleys. In my opinion, the above considerations contribute to coming closer to a theoretical understanding of their erosional power. Above all, however, I believe that our ideas may help to understand the apparent coexistence of relatively weakly erosional valley glaciers on the one hand and very effective glaciers on the other. By doing so, we seek to contribute to a reconciliation by giving credence to both of the currently existing positions in the discussion on glacier erosion.

3 Regarding the transverse profile of glacial valleys

The above considerations were mainly directed towards an interpretation of those peculiarities that occur in the longitudinal profile of valleys shaped by glacial erosion. However, they are also relevant for assessing the cross-sections of such valleys. It is not surprising that the more or less developed U-shape of glacial valleys represents the ideal cross-section form generated by an ice stream pushing over its bed with imperfect deformability, the rigidity of which, at least under certain, frequently realised conditions, is so great that the internal friction of the particles against each other is greater than the external friction against the bed and valley walls. These characteristics also mean that such a flow would not adhere equally firmly to the valley walls everywhere. Even at the terminus it is often found that the body of ice is only imperfectly in contact with the ground, so that its load and friction are only exerting effects on parts of its base.

According to the observations from glacier tunnels on the Marmolata by Handl (1917) and further reports on this by von Klebelsberg (1948), similar considerations should also apply to the upper firn field area. The important observations on the formation processes of roche moutonnée at the base of the upper Grindelwald glacier by Carol (1943, 1947) suggest that the contact pressure of ice, which varies from place to place during glacier movement over uneven ground, and is increased by the occurrence of pressure liquefaction and consequent increased plasticity of the ice, generally varies to a considerable extent. The overall result from assessing the interaction between a moving ice body with its bed and valley sides, which undoubtedly varies from place to place, must without question yield an explanation for the development of a U-shapes cross-section.

There has been much debate about whether the U-shape originates from a formerly V- or __/-shaped valley crosssection, and if this was caused primarily by erosion on the valley side walls or the valley floor. It is difficult to give a general answer to this question. Certainly, cases of predominant vertical erosion and predominant lateral erosion can be realised side by side with varying frequency and intensity, without it being possible in every case to prove the predominance of one or the other (hence the suggestion of both possibilities in the ideal profile Fig. 2). On the one hand, the development of an overdeepened rock trough under a valley step in a glacial valley is unmistakable proof of strong vertical erosion of the glacier. However, there are also cases in which the bottom of a trough is filled with moraine material and a more V-shaped valley floor is largely maintained. In these cases, the formation of a trough is more likely to be due to erosion of the glacier on the valley sides. In view of the theory of glaciers enhancing pre-existing slope breaks, one may assume that the formation of a trough shape above a valley step is likely due to preeminent glacial erosion on the valley sides, whereas if this shape occurs at the foot of the valley step it is more likely due to a greater extent to vertical glacial erosion.

It seems appropriate to apply our ideas on the material consistency of glaciers also to investigate irregularities in the transverse profile of glacial valleys. We encounter these in features such as glacial trimlines (German "Schliffgrenze"), "Schliffkehle", "Schliffbord"³ and rock scholder ("Trogschulter"). There is general agreement on understanding glacial trimlines as the upper limit of the ice flow moving laterally along the valley flanks and scouring it. However, less attention has been paid to the inherent consequences that can be derived from the specific range of land forms on or at the trimline. These, as is well known, comprise the following (Figs. 2 and 3):

The ragged shape, resulting from subaerial weathering, of many secondary ridges which descend from the main ridge, take on a more rounded form from a certain altitude down-

³TN: There is no direct equivalent for these two terms in English. "Schliffkehle" = hollow/steep part below the trimline; "Schliffbord" gently inclined upper part of the slope (see Figs. 2 and 3).



Figure 2. Schematic cross-section of a trough valley with steep ice-moulded surfaces. Finely-dashed profile indicates the possible preglacial valley cross-section. Unbroken line of trough bottom corresponds to the assumption of shallow glacial erosion. Coarsely-dashed trough base corresponds to the assumption of a strong vertical component of glacial erosion.



Figure 3. Schematic transverse profile of a glacial trough with true trough shoulders. (The shoulder surfaces are shallower than the general ridge slope above the trimline. Their formation cannot be explained by the simple assumption of a gradual increase in glacial erosion from the trimline downwards. Roughly dashed: a possible form of the underlying preglacial valley profile showing trough terraces.)

wards. However, just above the point on the ridge where it transitions to a more rounded form, a noticeable steepening of the slope is usually discernible. As is well known, this finding prompted Albrecht Penck to give the name "Schliffkehle" to these features. However, as far as I know, it has not yet been clearly expressed that this finding can often be used to obtain information on the minimum size of the abrasive effect of the valley glacier moving roughly horizontally along the slope. This is possible when the mean slope of the ridge line of the secondary ridge above the gully steepening is so moderate that this ridge line experiences a clear bend through the recessed slope bend of the gully steepening (cf. Fig. 2).

Such sudden downshifting of the general hanging profile at the cut boundary is very common. The magnitudes involved usually range from several metres to tens of metres. They indicate the amount by which the abrasive action of the valley glacier moving along the slope at its upper margin has preceded the ablative action of subaerial weathering and denudation in the area rising above the glacier surface, thus producing the recessed angle on the slope. The often-observed general lowering of the slope profile below the trimline shows that the so-called black-white boundary may play an additional but not a dominant role in the formation of the "Schliffkehle". If the "Schliffkehle" was only a groove cut into the slope at the level of the ice flow, then the glacially shaped and polished surfaces below the trimline should approximately represent the imaginary lower continuations of the slopes above the steepening of the "Schliffkehle". As a rule, however, they lie much lower than these imaginary continuations (cf. the suggestion of these conditions in Fig. 2).

From the appreciation of the high rigidity of the nearsurface layers of the moving glacier ice, it could theoretically be concluded that in the glacial accumulation area, i.e., above the area of deposition of moraine material, the abrasive effect of the glacier must already begin at the valley margins with considerable force. In any case, there is little to suggest that the erosional effect decreases to zero towards the edge of the glacier, as could be inferred based on the concept of glaciers as a viscous fluid in which the speed of movement approaches zero towards the edge. Overall, the observations of the "Schliffkehle" indicate that glacial valleys were primarily formed by glaciers whose movement was of the block floe type or at least related to it.

If erosive processes by glaciers already commence at the high lateral valley sides (trimlines), then it must be assumed that erosion occurs with even greater effect at depth, in which ice mass are pushed along the walls and bed under yet greater pressure. Thus, in the transverse profile of the glacier bed, one can expect an increasing amount of erosion of the ice downwards along the valley walls to the bed. Yet, it cannot be determined whether the erosional maxima occur directly at the valley depth line, or if the maxima occur higher on the valley sides with the erosional capacity decreasing towards the depth line itself. As already discussed, both situations, that of predominant vertical erosion and that of predominant lateral erosion on the valley slopes, certainly do occur.

The idea of an increase in glacial erosion from the lateral margin into the depth of the central valley appears to be an important aspect for distinguishing between the entire icemoulded area and the trough shoulder, which has not always been conducted with the desirable degree of attention. Quite often one finds broad, strongly inclined, smoothed surfaces developed below the ground grooves, which are noticeably flatter than both the steppened sections immediately above the "Schliffkehle" and the actual trough walls further down. In such cases, the question arises whether these features represent strongly over-printed pre-existing (old) valley floor remnants, i.e., genuine trough shoulders?

If we bear in mind that the probable cross-section of a previously straight or slightly convex slope (Fig. 2), reworked by a passing valley glacier, showing a steepening above the "Schliffkehle", and then continuing below the "Schliffkehle" almost parallel to the original angle of slope, but again gradually steepening downwards, until it finally merges into the actual trough walls, we see the possibility of explaining such forms without the aid of postulating the presence of old valley floor remains. Especially when the slope of the rounded areas below the trimline, but above the trough walls, is as great or greater than the average slope of the slope or the crest line of the secondary ridges, which rise above the ridge caused by the groove boundary to the main ridge, there is no reason to think of old valley floor remains as the cause of these areas of more moderate slope above the actual trough walls. They are undoubtedly merely abrasion ridges, i.e., areas which have been removed by the ice flowing past, and which merge downwards into the trough walls as a result of the increased abrasion work of the ice. Von Drygalski (1912), Philippson (1912) and others have put forward a number of arguments for this. Such ice-moulded terrain, which to all appearances does not derive from old valley floor remains, is more frequent in the Alps than is generally assumed, as a closer examination of many slope profiles has shown to me. This is also indicated by von Klebelsberg (1948: p. 353).

Only when the ice-covered areas above the trough walls have a lower inclination than the slope above the trimlines, or than the ridge lines of the secondary ridges leading up from there to the main ridge (Fig. 3), is it possible to conclude with some certainty that old slope segments or valley floor remnants are present. In such cases they are real trough shoulders. The fact that such trough shoulders actually occur, even several of them on top of each other, and can be shown to be over-printed remnants of old valley floors, has been certain since the work by Lautensach (1912) in Ticino and has also been proven in many other cases.

But it seems to me that so far not enough attention has been paid to the distinction between two fundamentally different trough cross profiles: the true trough shoulder profile with rather flat shoulder surfaces and the ground slope profile with much steeper slopes above the actual trough. The trough shoulder profiles are most often found in glacial landscapes where pronounced altitudinal levels exist ("Gipfelflur"), with a middle or low relief at the top and abrupt valley notches below. The trough shoulder profiles are most often found in glacial landscapes with a pronounced vertical structure, with a middle or low relief at high altitude and abrupt valley thresholds below. Trimlines are found mainly in areas with high, moderately steep average slopes. If the slopes in deeply-eroded mountains are even too steep, the type of allvalley troughs described by Distel (1912) results from strong valley glaciation.

Here it should be pointed out that a trough profile with a steep ice-moulded area can be derived without further difficulty from the glacial reshaping of a previously existing simple groove or bed valley. This is based on the physically probable assumption that the erosion of the valley glacier starts at the trimline with a certain amount, that it initially increases downslope towards the base of the bed until it reaches a maximum, and that it can then possibly decrease again towards the centre of the bed. The deepening of the profile at the crevasse throat gives an indication of the minimum erosion work carried out by the glacier at the edge.

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